Abstract—Image fusion is a technique that combines two source images to generate more informative target image. It plays a vital role in medical image investigation, military, navigation, etc. visible images offer efficient texture detail with high spatial resolution. In contrast, based on the radiation difference infrared images are able to differentiate target from their background. There are many algorithms that helps in preserving the edges of image like Bilateral filter, Anisotropic Diffusion (ADF). This paper proposes a novel approach by integrating Anisotropic Diffusion and Karhunen-Loeve (KL) Transformation with Discrete Wavelet Transform (DWT). In proposed Method, DWT decomposes into four sub-bands. ADF is applied on approximation sub-band and absolute maximum selection is applied on other three sub-bands. ADF decomposes the image into detailed layer and base layer. Base layer and Detailed layer are calculated using Kl- Transformation and linear combination respectively. Once fusion is done, inverse DWT is applied on all sub-bands. The experimental outcomes depict that the offered approach result with sharp edges of the image. The proposed algorithm is evaluated on standard dataset Like Duine_Sequence, Tree_Sequence, Street dataset. Standard metrics like Average Gradients and Spatial Frequency metrics are used to evaluate the performance of the image. The results depict that the proposed approach outperforms state of the art approaches on various datasets.

Index Terms—Image fusion, Infrared and Visible image, DWT, Anisotropic Diffusion.

I. INTRODUCTION

Image fusion is a procedure that targets to integrate two images attained by one or more different kinds of sensor to achieve an informative image. This information is useful in decision making [1]. In recent years, research on image fusion has been growing rapidly. The enhanced vision system, medical diagnosis, robotics, military, surveillance, object identification [2] [3], classification and change detection are the application of image fusion [4].

Image fusion can be applied to various source images like infrared and visible bands, Panchromatic (PAN) and Multispectral (MS) bands. Infrared and visible band images have many aspects.

Visible band images represent the spatial information of the fused image and also contains the texture detail of the scene and edges details [5]. In contrast, infrared images have an advantage over the uncovering of the fused image. It can also work efficiently under the illness of night vision, bad weather and weak light [5]. The focus of this paper is on the fusion of Visible and Infrared band images.

Image fusion can be categorized as depicted in Fig. 1

Fig. 1. Classification of Image Fusion

Pixel-level image fusion works directly on the spatial information (pixel intensity) of the image [6]. In Feature-level image fusion, features are extracted from the source image [6]. Decision-level image fusion is a high level of image fusion, integrates the outcomes from multiple technique to proceeds a final fused decision [7]. Pixel-level image fusion is further categorized into transform domain [8] and spatial domain [8]. Image fusion in spatial domain deal with pixel intensity of the input image. In contrast, image fusion in transform domain works with the frequency representation of an image.

Image fusion is an essential area in an information science. Over the past decade, various different algorithms are introduced, each having their own methodology. Edge-preserving smoothing is an image processing procedure that smooth away from noise or texture and retaining the sharp edges. Recently, there are many edge preserving techniques used for image fusion that includes weighted least square filter.
The rest of this work is organized as follows. An overview on image fusion techniques is described in section II. The proposed method is described in section III. Section IV showcases the performance of the proposed approach on standard datasets evaluated it by comparing it with other competitive methods. Section V contains a conclusion.

II. OVERVIEW OF IMAGE FUSION METHOD

An outline of Image Fusion method using state of the art anisotropic diffusion is depicted in Fig. 2.

![Fig. 2. Schematic of ADF algorithm and KL Transformation apply on image fusion](image)

Fig. 2 represents decomposition of source images into base layer and detailed layer via ADF. Firstly, ADF extract the base layer of the source images. Detailed layer is obtained by subtracting base layer from source images. Base layer and detailed layer calculated with the KL - Transformation and linear combination respectively. Finally calculate the inverse of image and get the fused image.

The ADF [14] is control the diffusion of image by using flux function. For that the equation of ADF is given below:

\[
\frac{\partial I}{\partial t} = \text{div}(c(x,y,t) \nabla I) \tag{1}
\]

\[
I_t = \nabla c \cdot \nabla I + c(x,y,t) \nabla I \tag{2}
\]

where, \( I \) = image, \( \nabla \) = gradient operator, \( \Delta \) = laplacian operator, \( t \) = iteration or scale or time, \( c(x,y,t) \) is the diffusion coefficient.

Eq. 2 referred as a heat equation. The solution for this PDE is calculated by using Forward Time Central Space (FTCS).

\[
I_{ij}^{t+1} = I_{ij}^t + \lambda [c_E \nabla_E I + c_W \nabla_W I + c_N \nabla_N I + c_S \nabla_S I] \tag{3}
\]

where, \( \lambda \) is constant between 0 \( \leq \lambda \leq \frac{1}{\varepsilon} \). \( I_{ij}^{t+1} \) is coarser resolution image at \( t + 1 \) Image. \( I_{ij}^t \) is previous coarser image. \( \nabla_E, \nabla_W, \nabla_N, \nabla_S \) indicates nearest-neighbour differences and is calculated as below in East, West, North and South directions respectively.

\[
\nabla_E I_{ij} = I_{ij} + 1 - I_{i,j} \]

\[
\nabla_W I_{ij} = I_{ij} - 1 - I_{i,j} \]

\[
\nabla_N I_{ij} = I_{i-1,j} - I_{i,j} \]

\[
\nabla_S I_{ij} = I_{ij} + 1 - I_{i,j} \tag{4}
\]

Likewise, flux or conduction coefficients \( c_E, c_W, c_N, c_S \) are updated during every iteration in different directions is defined as below:

\[
c_E^t = \frac{\| (\nabla I)_{i,j+1} \|}{\| (\nabla I)_{i,j} \|} \tag{5}
\]

\[
c_W^t = \frac{\| (\nabla I)_{i,j-1} \|}{\| (\nabla I)_{i,j} \|} \tag{6}
\]

\[
c_N^t = \frac{\| (\nabla I)_{i-1,j} \|}{\| (\nabla I)_{i,j} \|} \tag{7}
\]

\[
c_S^t = \frac{\| (\nabla I)_{i+1,j} \|}{\| (\nabla I)_{i,j} \|} \tag{8}
\]

Here, \( g(\cdot) \) is decreasing function with \( g(0) = 1 \). Distinct functions can be used for \( g(\cdot) \). Perona and Malik [12] recommended two function as below:

\[
g(\nabla I) = \frac{1}{1 + (\frac{\| \nabla I \|}{k})^2} \tag{6}
\]

\[
g(\nabla I) = e^{-\frac{(\| \nabla I \|)^2}{k}} \tag{7}
\]

In both functions, constant \( k \) is used for determine the validity of a region boundary based on its edge strength.

One of the most popular techniques is wavelet transform based techniques. Wavelet theory is frequency based techniques that enhances the result of image by changing the low-frequency and high frequency parameter. DWT [16], [17], [18], is a most popular technique in information science that is used to retrieve multi-resolution of image.

![Fig. 3. Decomposition of image](image)
As shown Fig. 3 DWT decomposes image in four sub bands. Initially, image is decomposed using row-wise DWT which results into low frequency and high frequency details. Both are further decomposed using column-wise DWT that results into four sub bands. These four bands are Approximation band (LL), Vertical band (LH), Horizontal band (HL) and Diagonal band (HH).

Fig. 4. illustrates decomposition of images into four sub bands using DWT. An average of LL subband of visible and infrared is computed. Also, maximum of LH, HL and HH bands are computed of visible and infrared Images. Finally, apply inverse dwt on the image and retrieve final fused image.

The scaling function \( \phi(t) \) and wavelet function \( \psi(t) \) of DWT is illustrated as below:

\[
\phi(t) = \sum_{k=-\infty}^{\infty} (p_k)Q(2t - k) \tag{8}
\]

\[
\psi(t) = \sum_{k=-\infty}^{\infty} (q_k)Q(2t - k) \tag{9}
\]

The haar wavelet transform is one of the simplest transforms and sequence of rescaled "square-shaped" functions in wavelet family. The scaling function \( \phi(t) \) and mother wavelet function \( \psi(t) \) of haar wavelet [16], [17], \( p_k \) and \( q_k \) are represented as low pass and high pass filter respectively.

\[
\phi(t) = \begin{cases} 
-1, & 0 \leq t < 1 \\
0, & \text{otherwise}
\end{cases} \tag{10}
\]

\[
\psi(t) = \begin{cases} 
1, & 0 \leq t < 1/2 \\
-1, & 1/2 \leq t < 1 \\
0, & \text{otherwise}
\end{cases} \tag{11}
\]

III. PROPOSED APPROACH

Related work represents functioning of ADF and DWT and recent approaches towards it. By using Partial Differential Equation (PDE), ADF [12] preserves nonhomogeneous regions (edges) and it smooths homogeneous regions. DWT provides multiresolution of image and it also provides perfect image reconstruction. However, ADF individually is not able to preserve the edges while completely removing the noise using the ADF after some extent. Similarly, DWT also has some challenges such as less directional selectivity, shift invariance, aliasing, oscillation of wavelet coefficients. This paper proposes an efficient method that overcomes limitations in both state of the art techniques.

The image is decomposed into four sub bands. Average is computed of approximation band of two images. Anisotropic diffusion with KL-transformation on the resulting approximate image. The approximation band and other three sub bands of two images are integrated. Finally, inverse DWT is computed on integrated images to achieve final efficient fused image.
The input Approximation band (LL) of images \( I_n(p, q) \) with \( R \times S \) size all are registered. Now, Anisotropic diffusion is applied on that to get base layers.

\[
b_n(p, q) = \text{anisotropic} \ (I_n(p, q))
\]

where, \( b_n(p, q) \) is the \( n^{th} \) base layer and anisotropic \((I_n(p, q))\) denotes the anisotropic diffusion process on the \( n^{th} \) input images and \( p \) and \( q \) denotes the pixel values.

To get detailed layer from Approximation band (LL) of images, subtract base layer from input images.

\[
d_n(p, q) = I_n(p, q) - b_n(p, q)
\]

where, \( d_n(p, q) \) is the \( n^{th} \) detailed layer of the \( n^{th} \) input image.

Weighted superposition is computed on Base layer. This is retrieved by allocating some weight \( w_n \) to images. This can be represented as:

\[
B_n = w_n \sum_{n=1}^{N} b_n(p, q)
\]

where \( 0 \leq w_n \leq 1 \) and \( \sum w_n = 1 \).

Here, for \( \forall n, w_1, w_2, w_3, \ldots \ldots w_N = \frac{1}{N} \) represents the average of Base Layer.

Calculate detail layers using KL transform [9]. It converts the correlated components into the uncorrelated components [10].

This is computed using following steps.

A.1 ADF algorithm is applied on various Approximation band (LL) of \( N \) images. There are two input images \( I_1(p, q) \) and \( I_2(p, q) \) having two detailed layers \( d_1(p, q) \) and \( d_2(p, q) \) respectively. These detail layers are placed as column vectors of a matrix \( A \).

A.2 Calculate the covariance matrix \( C_{aa} \) of \( A \) in terms of each column as a variable and each row as an observation.

A.3 Calculate Eigen values \( C_1, C_2 \) and Eigen vector \( V_1, V_2 \) of \( C_{aa} \).

\[
V_1 = \begin{bmatrix} V_1(1) \\ V_1(2) \end{bmatrix}, \quad V_2 = \begin{bmatrix} V_2(1) \\ V_2(2) \end{bmatrix}
\]

A.4 Eigen vector \( V_{\text{max}}(i) \) is computed corresponding to the large Eigen values \( C_{\text{maximum}} = \text{maximum} (C_1, C_2) \).

A.5 Uncorrelated components \( KL_1 \) and \( KL_2 \) are computed as below:

\[
KL_1 = \frac{V_{\text{max}}(1)}{\sum V_{\text{max}}(1)} \quad KL_2 = \frac{V_{\text{max}}(2)}{\sum V_{\text{max}}(2)}
\]

A.6 The final fuse detailed layer \( D \) is retrieved as below:

\[
D(p, q) = KL_1 d_1(p, q) + KL_2 d_2(p, q)
\]

A.7 For \( n \) detail layer the generalized equation is

\[
D(p, q) = \sum_{n=1}^{N} d_n(p, q) \quad KLL_n
\]

By using a simple linear combination of Base layer and the Detailed layer, final fuse Approximation band (LL) of image is retrieved.

\[
F = B + D
\]

Once the approximate band is integrated with ADF. HL, LH and HH bands of images are computed. The coefficients of HL, LH, HH bands of two images are computed using choose-max rule as below.

\[
Hf(i,j) = \begin{cases} HL_1(i,j) & \text{Others} \\ HL_2(i,j) & \text{Others} \end{cases}
\]

\[
Vf(i,j) = \begin{cases} VL_1(i,j) & \text{Others} \\ VL_2(i,j) & \text{Others} \end{cases}
\]

\[
Df(i,j) = \begin{cases} DL_1(i,j) & \text{Others} \\ DL_2(i,j) & \text{Others} \end{cases}
\]

Lastly, inverse DWT is applied on fused coefficient to retrieve final fused image.

IV. SIMULATION RESULTS

In this paper, the proposed algorithm is evaluated on standard dataset such as tree_sequence [20], duine_sequence [20], and street [21].

![Fig. 6. Duine_Sequence Dataset: (a) Original Infrared Image (b) Original Visible Image (c) Result of DWT (d) Results of Anisotropic. (e) Results of DWT with Anisotropic.](image)
standard parameter are used to measure the image quality. These standard parameters are spatial frequency [1] and average gradients [19].

\[ SF = \sqrt{RF^2 + CF^2} \]

where, CF and RF is Column Frequency and Row Frequency respectively.

\[ RF = \frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=2}^{N} [F(i,j) - F(i,j-1)]^2 \]

\[ CF = \frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=2}^{N} [F(i,j) - F(i-1,j)]^2 \]

where, F = given image, (i,j) = Pixel Index, f(i,j) = gray value at pixel (i,j), M = number of rows, N = number of column. The huge SF of fused image is more informative in terms of edges and texture.

B. Average Gradients

The average gradients (AG) [18] computed as follow:

\[ AG = \frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=1}^{N} [\Delta pf(i,j)^2 + \Delta qf(i,j)^2]^\frac{1}{2} \]

where, \( \Delta pf \) and \( \Delta qf \) is the difference value of pixel in p or q direction. M denotes the number of rows and N denotes the number of columns. It is used to define the minor changes of detailed contrast and variation of texture information.

C. Entropy

Entropy utilizes the basis of information theory to estimate the amount of information contained in a fused image on the basis of information theory The Entropy (ET) [18] can be computed as follows:

\[ EN = - \sum_{l=0}^{L-1} H_l \log_2 H_l \]

where, \( L \) represents the occurrences of gray levels and \( H_l \) is the normalized histogram of the corresponding gray level in the fused image. The higher value of EN depicts more information enclosed in the fused image. It also represents the efficient performance of the fusion technique.

D. Mutual Information

The Mutual Information (MI) [18] can be computed as follow:

\[ MI = MI_{vis,fus} + MI_{inf,fus} \]

\( MI_{vis,fus} \) and \( MI_{inf,fus} \) represents the information transferred from visible as well as in frared images to the fused image. The MI amongst two random variables can be estimated by the standard Kullback-Leibler measure as follow:

\[ MI_{X,fus} = \sum_{X,F} H_{X|F}(X,F) \log \frac{H_{X,fus}(X,F)}{H_X(X)H_F(F)} \]
H(F) represents the marginal histograms of input image X and fused image F, respectively. H(F) represents the joint histogram of input image X and fused image F. A high MI metric represents that substantial information is transferred from input images to the fused image. This also depicts an efficient fusion performance.

Table I represents results of the state-of-the-art methods and proposed approach on standard dataset using standard evaluation parameter. Percentage increase indicates the quality increased in percentage of proposed method as in compare with highest state of the art method.

<table>
<thead>
<tr>
<th>Image Dataset</th>
<th>PM</th>
<th>DWT</th>
<th>ADF</th>
<th>ANI DWT</th>
<th>% Increase</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>SF</td>
<td>3.0414</td>
<td>1.9895</td>
<td>3.0592</td>
<td>0.585257</td>
</tr>
<tr>
<td>Dataset</td>
<td>AG</td>
<td>21.6511</td>
<td>10.2932</td>
<td>21.8092</td>
<td>0.730217</td>
</tr>
<tr>
<td>Diine_</td>
<td>ET</td>
<td>5.8044</td>
<td>5.7689</td>
<td>5.8057</td>
<td>0.022397</td>
</tr>
<tr>
<td>Sequence</td>
<td>MI</td>
<td>11.6088</td>
<td>11.5738</td>
<td>11.6114</td>
<td>0.022397</td>
</tr>
<tr>
<td>Dataset</td>
<td>SF</td>
<td>2.3493</td>
<td>1.6885</td>
<td>2.3538</td>
<td>0.191546</td>
</tr>
<tr>
<td></td>
<td>AG</td>
<td>19.7909</td>
<td>12.1065</td>
<td>19.7995</td>
<td>0.043454</td>
</tr>
<tr>
<td>Tree_</td>
<td>ET</td>
<td>5.9472</td>
<td>5.9117</td>
<td>5.9486</td>
<td>0.023540</td>
</tr>
<tr>
<td>Sequence</td>
<td>MI</td>
<td>11.8944</td>
<td>11.8235</td>
<td>11.8971</td>
<td>0.0227</td>
</tr>
<tr>
<td>Dataset</td>
<td>SF</td>
<td>3.5923</td>
<td>2.3690</td>
<td>3.5961</td>
<td>0.105782</td>
</tr>
<tr>
<td></td>
<td>AG</td>
<td>30.5306</td>
<td>14.5847</td>
<td>30.5842</td>
<td>0.175562</td>
</tr>
<tr>
<td>Street</td>
<td>ET</td>
<td>5.9575</td>
<td>5.9192</td>
<td>5.9575</td>
<td>0.000039</td>
</tr>
<tr>
<td>Dataset</td>
<td>MI</td>
<td>11.9149</td>
<td>11.8383</td>
<td>11.9150</td>
<td>0.000039</td>
</tr>
</tbody>
</table>

The proposed algorithm accuracy outperforms state-of-the-art algorithms in terms of standard evaluation metrics such as Spatial Frequency (SF) and Average Gradients (AG).

V. CONCLUSION

A novel approach is suggested in this paper, with a focus to improve the performance of fused image and to highlight the object of image. This algorithm is based on integrating the ADF and DWT. Firstly DWT decomposes the image into four sub bands LL, LH, HL, HH respectively. ADF algorithm is applied on LL sub bands and absolute maximum selection is applied on other three sub bands. Finally perform the inverse DWT of the image is computed to retrieve the fused image. The outcomes attained during the experiment, illustrates that proposed algorithm is better than state-of-the-art algorithm with regards of preserving the edge information of the image. In future, the proposed algorithm can be extended for panchromatic and multispectral image.

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